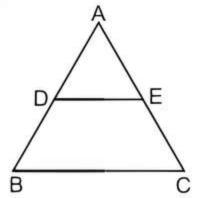
Fastrack Revision

- Similar Figures: Two figures having the same shapes (and not necessarily the same size) are called similar figures.
- Similar Triangles: Two triangles are said to be similar if:
 - 1. their corresponding angles are equal.
 - 2. their corresponding sides are in the same ratio (or proportional).

Note: Suppose $\triangle ABC$ is similar to $\triangle PQR$, we write as ΔABC ~ ΔPQR. But we do not write as ΔABC ~ ΔQRP or $\triangle BAC \sim \triangle PQR$.

- ▶ Equiangular Triangles: If corresponding angles of two triangles are equal, then they are equiangular triangles. The ratio of any two corresponding sides of each pair in two equiangular triangles is always the same.
- ▶ Basic Proportionality Theorem—BPT (Thales' Theorem): In a triangle, a line drawn parallel to one side, to intersect the other two sides at distinct points, divides the two sides in the same ratio. In \triangle ABC, DE || BC, then $\frac{AD}{DB} = \frac{AE}{EC}$,



$$\frac{AD}{AB} = \frac{AE}{AC}$$
 and $\frac{AB}{DB} = \frac{AC}{EC}$

- ▶ Converse of Basic Proportionality Theorem: If a line divides any two sides of a $\triangle ABC$ in the same ratio, i.e., $\frac{AD}{DB} = \frac{AE}{EC}$, then the line must be parallel to the third side, i.e., DE || BC.
- ▶ Criterion for Similarity of Triangles: There are three criteria for similarity of triangles :
 - 1. AAA Similarity: In two triangles, if three angles of one triangle are respectively equal to the three angles of the other triangle, then the two triangles are similar.

If two of their angles are equal, then the third angle must also be equal, because sum of angles of a triangle always make 180°. So, AA could also be called similarity.

2. SSS Similarity: In two triangles, if the corresponding sides are proportional, then they are similar.

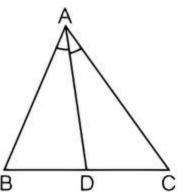
Or

In two triangles, if sides of one triangle are proportional to the sides of the other triangle, then their corresponding angles are equal and hence the two triangles are similar.

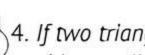
3. SAS Similarity: In two triangles, if one pair of corresponding sides are proportional and the included angles are also equal, then the two triangles are similar.

Knowledge BOOSTER

- 1. All congruent triangles are similar but the similar triangles need not be congruent.
- 2. Mid-point Theorem: The line segment joining the mid-points of any two sides of a triangle is parallel to the third side and is half of it.
- 3. Angle Bisector Theorem: The internal bisector of an angle of a triangle divides the opposite side in two segments that are proportional to the other two sides of the triangle.



In
$$\triangle ABC$$
, $\frac{A}{\Delta}$



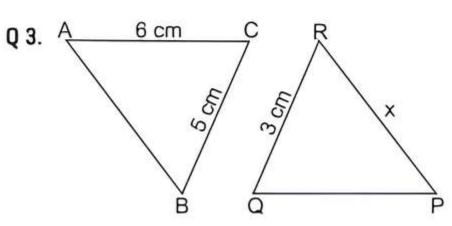
4. If two triangles are similar, then their corresponding sides, medians and altitudes are proportional.



Practice Exercise

Multiple Choice Questions >

- Q1. Two polygons have same number of sides are similar, if:
 - a. their corresponding sides are proportional
 - b. their corresponding angles are equal
 - c. Both a. and b.
 - d. None of the above
- Q 2. If $\triangle ABC \sim \triangle PQR$ with $\angle A = 32^{\circ}$ and $\angle R = 65^{\circ}$, then the measures of \angle B is: [CBSE 2023]
 - a. 32°
- b. 65°
- c. 83°
- d. 97°



In the given figure, $\triangle ABC \sim \triangle QPR$. If AC = 6 cm, BC = 5 cm, QR = 3 cm and PR = x, then the value of x is:

[CBSE 2023]

- a. 3.6 cm
- b. 2.5 cm
- c. 10 cm
- d. 3.2 cm

Q 4. If in \triangle ABC and \triangle PQR, we have

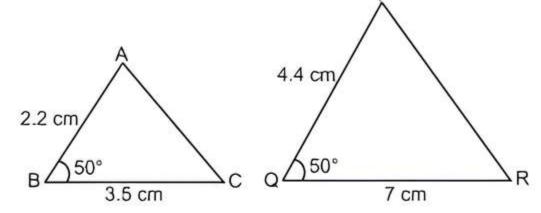
then: [CBSE SQP 2023-24, NCERT EXEMPLAR]

- a. $\Delta PQR \Delta CAB$
- b. ΔPQR-ΔABC
- c. ΔCBA- ΔPQR
- d. ΔBCA-ΔPQR
- Q 5. Which of the following is NOT a similarity criterion?

[CBSE SQP 2023-24]

- a. AA
- b. SAS
- c. AAA
- d. RHS

Q 6.

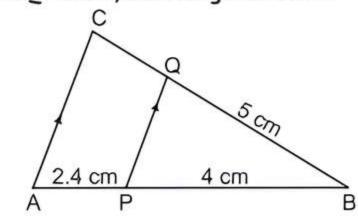


In the above figure, the criterion of similarity by which △ABC~△PQR is: [CBSE 2023]

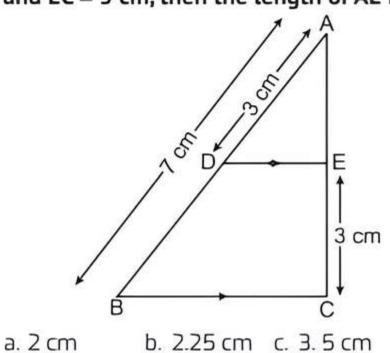
- a. SSA (Side-Side-Angle) similarity
- b. ASA (Angle-Side-Angle) similarity
- c. SAS (Side-Angle-Side) similarity
- d. AA (Angle-Angle) similarity
- Q 7. In a \triangle ABC, it is given that AB = 6 cm, AC = 8 cm and AD is the bisector of $\angle A$. Then, BD : DC =
 - a. 3:4
- b. 9:16
- c. 4:3

c. 3:2

- d. √3:2
- Q 8. \triangle ABC \sim \triangle PQR. If AM and PN are altitudes of \triangle ABC and $\triangle PQR$ respectively and $AB^2: PQ^2 = 4:9$, then AM : PN =[CBSE SQP 2021 Term-I]
 - a. 16 : B1
- b. 4:9
- d. 2:3
- Q 9. In the given figure, PQ \parallel AC. If BP = 4 cm, AP = 2.4 cm and BQ = 5 cm, then length of BC is: [CBSE 2023]

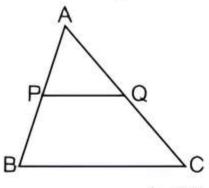


- a. 8 cm
- b. 3 cm
- c. 0.3 cm
- d. $\frac{25}{3}$ cm
- Q 10. In the given figure, DE \parallel BC. If AD = 3 cm, AB = 7 cm and EC = 3 cm, then the length of AE is: [CBSE 2023]



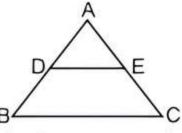
d. 4 cm

Q11. In \triangle ABC, PQ || BC. If PB = 6 cm, AP = 4 cm, AQ = 8 cm, find the length of AC. [CBSE 2023]



- a. 12 cm
- b. 20 cm
- c. 6 cm
- d. 14 cm
- Q 12. In $\triangle ABC$, DE || AB. If AB = a, DE = x, BE = b and EC = c. Express x in terms of a, b and c. [CBSE SQP 2023-24]
 - a. $\frac{ac}{b}$

 - d. $\frac{ab}{b+c}$
- Q 13. In the given figure, if DE \parallel BC, AD = 3 cm, BD = 4 cm and BC = 14 cm, then DE equals: [CBSE SQP 2021 Term-I]

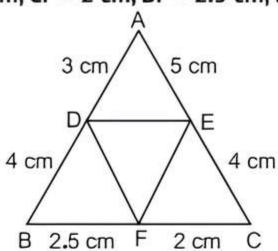


- a. 7 cm
- b. 6 cm
- c. 4 cm
- d. 3 cm
- Q 14. In $\triangle ABC$ and $\triangle DEF$, $\angle B = \angle E$, $\angle F = \angle C$ and AB = $\frac{1}{2}$ DE. Then, the two triangles are: [CBSE 2021 Term-I]
 - a. congruent but not similar
 - b. similar but not congruent
 - c. neither congruent nor similar
 - d. congruent as well as similar
- Q 15. It is given that $\triangle ABC \sim \triangle DFE$, $\angle A = 30^{\circ}$, $\angle C = 50^{\circ}$, AB = 5 cm, AC = 8 cm and DF = 7.5 cm. Then, which of the following is true? [NCERT EXEMPLAR]
 - a. DE = 12 cm, $\angle F = 50^{\circ}$
- b. DE = 12 cm, $\angle F = 100^{\circ}$
- c. EF = 12 cm, $\angle D = 100^{\circ}$ d. EF = 12 cm, $\angle D = 30^{\circ}$
- Q16. If the corresponding medians of two similar triangles are in the ratio 5:7, then the ratio of their corresponding sides is: [CBSE 2015]
 - a. 25:49
- b. 5:7
- c. 7:5
- d. 49:25
- Q 17. ABCD is a trapezium with AD || BC and AD = 4 cm. If the diagonals AC and BD intersect each other at O such that AO/OC = DO/OB = 1/2, then BC =

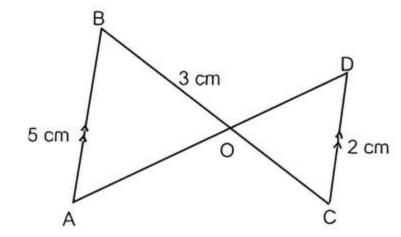
[CBSE SQP 2022-23]

- a. 6 cm
- b. 7 cm
- c. B cm
- d. 9 cm

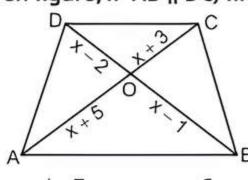
Q 18. In the given figure, AD = 3 cm, AE = 5 cm, BD = 4 cm, CE = 4 cm, CF = 2 cm, BF = 2.5 cm, then:



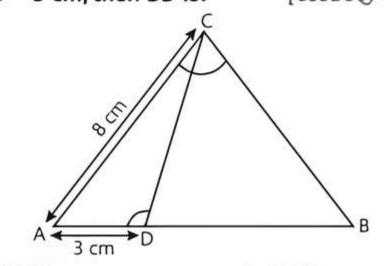
- a. DE II BC
- b. DF II AC
- c EF II AB
- d. None of these
- Q 19. It is given that, $\triangle ABC \sim \triangle EDF$, such that AB = 5 cm, AC = 7 cm, DF = 15 cm and DE = 12 cm, then the sum of the remaining sides of the triangles is:
 - a. 23.05 cm
- b. 16.8 cm
- c. 6.25 cm
- d. 24 cm
- Q 20. The sides of two similar triangles are in the ratio 4:7. The ratio of their perimeters is: [CBSE 2023]
 - a. 4:7
- b. 12:21
- c 16:49
- d. 7:4
- Q 21. In the given figure, AB || CD . If AB = 5 cm, CD = 2 cm and OB = 3 cm, then the length of OC is: [CBSE 2023]



- a. $\frac{15}{2}$ cm
- b. 10 cm
- $c. \frac{6}{5} cm$
- d. $\frac{3}{5}$ cm
- Q 22. In the given figure, if AB \parallel DC, find the value of x.



- a. 5
- b. 7
- c. 6
- d. 4
- Q 23. In the given figure, if $\angle ACB = \angle CDA$, AC = 8 cm, AD = 3 cm, then BD is: [CBSE SQP 2021 Term-I]



- a. 22/3 cm
- b. 26/3 cm
- c. 55/3 cm
- d. 64/3 cm

- Q 24. A vertical stick 12 m long casts a shadow 8 m long on the ground. At the same time, a tower casts the shadow 40 m long on the ground. Then, the height of the tower is:
 - a. 65 m
- b. 60 m
- c. 70 m
- d. 72 m



Assertion & Reason Type Questions >

Directions (Q.Nos. 25-29): In the following questions given below, there are two statement marked as Assertion (A) and Reason (R). Read the statements and choose the correct option:

- a. Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A)
- b. Both Assertion (A) and Reason (R) are true, but Reason (R) is not the correct explanation of Assertion (A)
- c. Assertion (A) is true but Reason (R) is false
- d. Assertion (A) is false but Reason (R) is true
- Q 25. Assertion (A): All regular polygons of the same number of sides such as equilateral triangles, squares etc, are similar.

Reason (R): Two polygons of the same number of sides are said to be similar, if their corresponding angles are equal and lengths of corresponding sides are proportional.

Q 26. Assertion (A): In a \triangle ABC, if DE || BC and intersects AB at D and AC at E, then $\frac{AB}{AD} = \frac{AC}{AE}$.

Reason (R): If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, then these sides are divided in the same ratio.

Q 27. Assertion (A): If the bisector of an angle of a triangle bisects the opposite side, then the triangle is isosceles.

Reason (R): The internal bisector of an angle of a triangle divides the opposite side internally in the ratio of the sides containing the angle.

Q 28. Assertion (A): In a $\triangle ABC$, D and E are points on sides AB and AC respectively such that BD = CE. If $\angle B = \angle C$, then DE is not parallel to BC.

Reason (R): If a line divides any two sides of a triangle in the same ratio, then the line must be parallel to the third side.

Q 29. Assertion (A): In \triangle ABC, DE || BC, such that AD = (7x-4) cm, AE = (5x-2) cm, DB = (3x+4) cm and EC = 3x cm then x is equal to 5.

Reason (R): If a line is drawn parallel to one side of triangle to intersect the other two sides at a distinct point, then the other two sides are divided in the same ratio.



Fill in the Blanks Type Questions >

- Q 30. Two triangles are similar, if their corresponding [NCERT EXERCISE; CBSE 2020] sides are
- Q 31. In $\triangle ABC$ and $\triangle DEF$, if $\angle B = \angle E$, $\angle F = \angle C$ and AB = 2DE. Then, the two triangles are
- Q 32. If in two triangles DEF and PQR, $\angle D = \angle Q$ and $\angle R = \angle E$, then $\frac{DE}{OR} = \frac{DF}{PO} = \dots$
- Q 33. The line segment joining the mid-points of any two sides of a triangle is to the third side.
- Q 34. All congruent triangles are similar but the similar triangles need not to be



True/False Type Questions >

- Q 35. If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, the other two sides are divided in the same ratio. [NCERT EXEMPLAR]
- Q 36. If AD and PM are medians of \triangle ABC and \triangle PQR respectively, where \triangle ABC \sim \triangle PQR, then $\frac{AB}{PO} = \frac{AD}{PM}$.
- Q 37. In two triangles, if one pair of corresponding sides are proportional and the included angles are also equal, then two triangles are similar.

Solutions

- 1. (c) Two polygons of the same number of sides are similar if their corresponding angles are equal and their corresponding sides are in the same ratio i.e. proportional.
- (c) Given ΔABC ~ ΔPQR

⇒
$$\angle A = \angle P$$
, $\angle B = \angle Q$ and $\angle C = \angle R$
∴ $\angle A = \angle P = 32^\circ$ and $\angle R = \angle C = 65^\circ$

Now, in $\triangle ABC$,

$$\angle A + \angle B + \angle C = 180^{\circ}$$

 $32^{\circ} + \angle B + 65^{\circ} = 180^{\circ}$

- $\angle B = 180^{\circ} 97^{\circ} = 83^{\circ}$
- 3. (b) Given, ΔABC ~ ΔQPR

$$\therefore \frac{AB}{QP} = \frac{BC}{PR} = \frac{CA}{RQ}$$

$$\Rightarrow \frac{BC}{PR} = \frac{CA}{RQ} \Rightarrow \frac{5}{x} = \frac{6}{3}$$

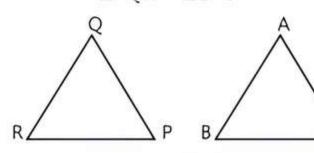
$$\Rightarrow$$
 $x = \frac{5 \times 3}{6} = \frac{5}{2} = 2.5 \text{ cm}$

4. (a) Given. In two $\triangle ABC$ and $\triangle PQR$. $\frac{AB}{OR} = \frac{BC}{PR} = \frac{CA}{PO}$

which shows that sides of one triangle are proportional to the side of the other triangle, then their corresponding angles are also equal, so by sss similarity, triangles are similar.



 $\Delta PQR \sim \Delta CAB$



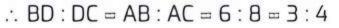
- 5. (d) AAA, AA, SSS and SAS all are similarity criterion of triangles while RHS is one of the congruency rule of triangles.
- **6.** (c) In $\triangle ABC$ and $\triangle PQR$, $\frac{AB}{PO} = \frac{BC}{OR} = \frac{1}{2}$

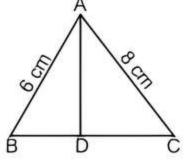
and
$$\angle B = \angle Q = 50^{\circ}$$

ΔABC ~ ΔPQR

By SAS (Side-Angle-Side) similarity criterion.

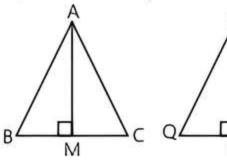
7. (a) We know that, the bisector of an angle of a triangle divides the opposite side in the ratio of the sides containing the angle.





[NCERT EXERCISE]

8. (d) Given, ΔABC ~ ΔPQR



If two triangles are similar, then their corresponding sides and altitudes are in same proportion.

AM and PN are altitudes of \triangle ABC and \triangle PQR respectively.

Also,
$$\frac{AB^2}{PQ^2} = \frac{4}{9} \implies \frac{AB}{PQ} = \frac{2}{3} \qquad ...(1)$$

As we know that,

Ratio of altitudes = Ratio of sides for similar triangles.

So,
$$\frac{AM}{PN} = \frac{AB}{PO} = \frac{2}{3}$$

9. (a) In \triangle ABC. PQ II AC

$$\frac{AP}{BP} = \frac{CQ}{BQ}$$

(By Thales theorem)

$$\Rightarrow \frac{2.4}{4} = \frac{CQ}{5}$$

$$\Rightarrow$$
 $CQ = \frac{2.4 \times 5}{4} = 3 \text{ cm}$

 \therefore Length of BC = BQ + CQ = 5 + 3 = 8 cm

10. (b) In ∆ ABC, BC || DE

$$\frac{AD}{BD} = \frac{AE}{CE}$$

(By Thales theorem)

$$\Rightarrow \frac{AD}{BD} + 1 = \frac{AE}{CE} + 1$$

$$\Rightarrow \frac{AD + BD}{BD} = \frac{AE + CE}{CE}$$

$$\Rightarrow \frac{AB}{AB - AD} = \frac{AE + CE}{CE}$$

$$\Rightarrow \frac{7}{7-3} = \frac{AE+3}{3}$$

$$\Rightarrow \frac{7}{4} = \frac{AE}{3} + 1$$

$$\Rightarrow \frac{AE}{3} = \frac{7}{4} - 1 = \frac{3}{4}$$

$$\Rightarrow AE = \frac{9}{4} = 2.25 \text{ cm}$$

11. (b) Given that.

In ∆ABC, PQ II BC

PB = 6 cm, AP = 4 cm, AQ = 8 cm

$$\therefore \frac{AP}{AB} = \frac{AQ}{AC}$$

$$\Rightarrow \frac{AP}{AP + PB} = \frac{AQ}{AC}$$

(By BPT)

$$\Rightarrow \frac{4}{4+6} = \frac{8}{AC} \Rightarrow \frac{4}{10} = \frac{8}{AC}$$

$$\Rightarrow AC = \frac{8 \times 10}{4} = 20 \text{ cm}$$

12. (b) Given AB = *a*. DE = *x*

$$BE = b$$
 and $EC = c$

In ΔABC, DE || AB

By basic proportionality theorem.

$$\Rightarrow \frac{DE}{ABC} = \frac{EC}{BC}$$

$$\Rightarrow \frac{DE}{AB} = \frac{EC}{BE + EC}$$

$$\Rightarrow \frac{x}{a} = \frac{c}{b+c} \Rightarrow x = \frac{ac}{b+c}$$

13. (b) Given, AD = 3 cm, BD = 4 cm, BC = 14 cm and DE II BC

$$\therefore$$
 \triangle ADE \sim \triangle ABC

(By AA similarity)

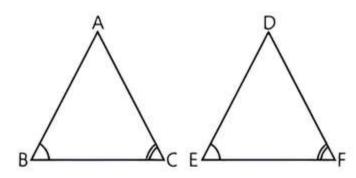
$$\Rightarrow \quad \frac{AD}{AB} = \frac{DE}{BC} \quad \Rightarrow \quad \frac{AD}{AD + BD} = \frac{DE}{BC}$$

$$\Rightarrow \frac{3}{3+4} = \frac{DE}{14} \Rightarrow DE = \frac{3 \times 14}{7} = 6 \text{ cm}$$

14. (b) In \triangle ABC and \triangle DEF.

$$\angle B = \angle E$$
, $\angle F = \angle C$ and $AB = \frac{1}{2}DE$

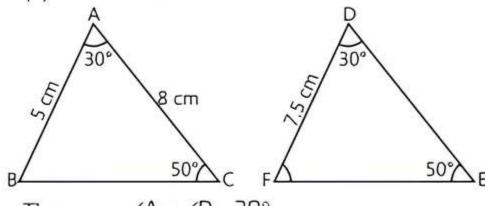
We know that, if in two triangles corresponding two angles are same, then they are similar by AA similarity criterion.



Since. AB ≠ DE

Therefore, $\triangle ABC$ and $\triangle DEF$ are not congruent.

15. (b) Given. $\triangle ABC \sim \triangle DFE$



Then.
$$\angle A = \angle D = 30^{\circ}$$
.

$$\angle C = \angle E = 50^{\circ}$$

$$\angle B = \angle F = 180^{\circ} - (30^{\circ} + 50^{\circ}) = 100^{\circ}$$

Also.
$$AB = 5$$
 cm, $AC = 8$ cm and $DF = 7.5$ cm

$$\frac{AB}{DF} = \frac{AC}{DE} \Rightarrow \frac{5}{7.5} = \frac{8}{DE}$$

$$\Rightarrow DE = \frac{8 \times 7.5}{5} = 12 \text{ cm}$$

Hence, DE = 12 cm. \angle F = 100°

16. (b) Let ABC and PQR be two similar triangles with medians AD and PS respectively.

$$\frac{AD}{PS} = \frac{5}{7}$$

(Given)

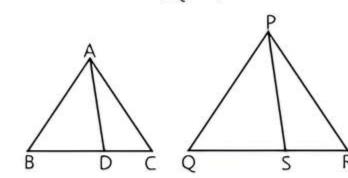
TR!CK-

The ratios of the medians of two similar triangles is equal to the ratio of their corresponding sides.

$$\Delta ABC \sim \Delta PQR$$

$$\frac{AB}{PQ} = \frac{AD}{PS}$$

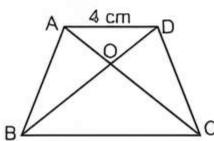
$$\frac{AB}{PO} = \frac{5}{7}$$



Hence, the ratio of corresponding sides is 5:7.

and
$$\frac{AO}{OC} = \frac{DO}{OB} = \frac{1}{2}$$

$$\frac{D}{C} = \frac{DU}{OB} = \frac{1}{2}$$
 ...(1)



In ΔAOD and ΔCOB

$$\angle ADO = \angle CBO$$

(: AD || BC, so alternate angles are equal) ∠ AOD = ∠ COB (Vertically opposite angles)

 \angle OAD = \angle OCB and

(Alternate angles are equal)

△ AOD ~ △COB (By AAA similarity rule)

(From eq. (1))

BC = B cm

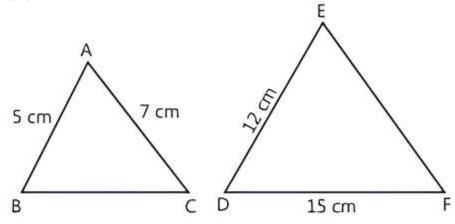
18. (c) Given, AD = 3 cm, AE = 5 cm, BD = 4 cm, CE = 4 cm, CF = 2 cm, BF = 2.5 cm

 $\frac{CF}{FB} = \frac{2}{2.5}$ Here $=\frac{20}{25}=\frac{4}{5}$

 $\frac{CE}{AE} = \frac{4}{5}$ and

(By converse of Thales theorem) EF II AB

19. (a) Given, ΔABC ~ ΔEDF



ΔABC ~ ΔEDF Since,

$$\therefore \frac{AB}{ED} = \frac{BC}{DE} = \frac{AC}{EE}$$

 $\frac{5}{12} = \frac{7}{FF} = \frac{BC}{15}$

On taking first and second ratios, we get

$$\frac{5}{12} = \frac{7}{EF} \implies EF = \frac{7 \times 12}{5} = 16.8 \text{ cm}$$

On taking first and third ratios, we get

$$\frac{5}{12} = \frac{BC}{15} \Rightarrow BC = \frac{5 \times 15}{12} = 6.25 \text{ cm}$$

Now, sum of the remaining sides of triangle.

= EF + BC = 16.8 + 6.25 = 23.05 cm

20. (a) Given, ratio of the sides of two similar triangles

w 4:7

TR!CK-If ΔPQR ~ ΔABC

 $\therefore \frac{PQ}{AB} = \frac{QR}{BC} = \frac{PR}{AC} = \frac{PQ + QR + PR}{AB + BC + AC}$

 $\Rightarrow \frac{PQ}{AB} = \frac{QR}{BC} = \frac{PR}{AC} = \frac{Perimeter of \triangle PQR}{Perimeter of \triangle ABC}$

.. Ratio of their perimeters = Ratio of the sides of two similar triangles = 4 : 7.

21. (c) In the given figure, AB IICD.

In \triangle COD and \triangle BOA,

 \angle OCD = \angle OBA [Alternate interior angles] [Alternate interior angles] \angle ODC = \angle OAB [Vertically opposite angles] and \angle COD = \angle BOA

Δ COD ~ ΔBOA

$$\frac{CO}{BO} = \frac{OD}{OA} = \frac{CD}{BA}$$

Given, AB = 5 cm, CD = 2 cm and OB = 3 cm

$$\Rightarrow \frac{CO}{BO} = \frac{CD}{BA} \Rightarrow \frac{CO}{3} = \frac{2}{5}$$
$$\Rightarrow CO = \frac{6}{5} \text{cm}$$

22. (b) Given, AB || DC

 $\angle ODC = \angle OBA$ and $\angle OCD = \angle OAB$

(Alternate interior angles) (Alternate interior angles)

ΔDOC ~ ΔΒΟΑ

(By AA similarity criterion)

Thus.
$$\frac{OD}{OB} = \frac{OC}{OA}$$

$$\Rightarrow \frac{x-2}{x-1} = \frac{x+3}{x+5}$$

$$\Rightarrow (x-2)(x+5) = (x+3)(x-1) \Rightarrow x^2 + 3x - 10 = x^2 + 2x - 3$$

x = 7

23. (c) Given, AC = 8 cm, AD = 3 cm

In \triangle ACD and \triangle ABC.

$$\angle CDA = \angle ACB$$
 (Given)
 $\angle CAD = \angle CAB$ (Common)

(By AA similarity) (By CPCT)

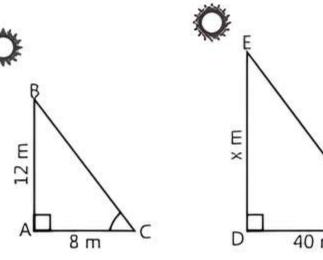
$$\frac{8}{\sqrt{8}} = \frac{3}{8}$$

 \Rightarrow

$$AB = \frac{64}{3} cm$$

So.
$$BD = AB - AD = \frac{64}{3} - 3 = \frac{55}{3} cm$$

24. (b) Let AB be the vertical stick and AC be its shadow. Also, let DE be the vertical tower and DF be its shadow. Join BC and EF. Let DE = x m



We have, AB = 12 m, AC = 8 m and DF = 40 mIn $\triangle ABC$ and $\triangle DEF$, we have

$$\angle A = \angle D = 90^{\circ}$$

(Angular elevation of the sun) $\angle C = \angle F$ (By AA similarity criterion) ΔABC ~ ΔDEF

$$\Rightarrow \frac{AB}{DE} = \frac{AC}{DF} \Rightarrow \frac{12}{x} = \frac{8}{40}$$

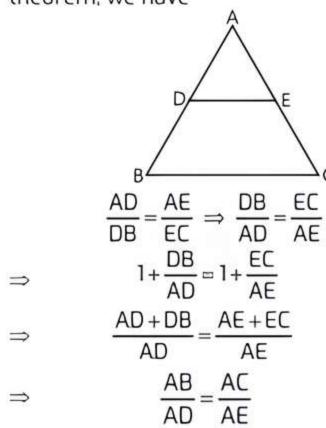
$$\Rightarrow \frac{12}{x} = \frac{1}{5} \Rightarrow x = 60 \text{ m}$$

- **25**. (a) **Assertion (A)**: Two polygons of the same number of sides are similar, if their corresponding angles are equal and corresponding sides are proportional.
 - : In equilateral triangles or squares, each angle is equal and sides are also proportional therefore all regular polygons are similar.

Reason (R): It is also true.

Hence, both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).

26. (a) Assertion (A): In ΔABC, DE II BC, by using Thale's theorem, we have



So, Assertion (A) is true.

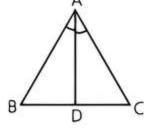
Reason (R): It is also true.

Hence, both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).

27. (a) Assertion (A): In \triangle ABC, AD is the bisector of \angle A.

$$\frac{AB}{AC} = \frac{BD}{DC}$$

$$\Rightarrow \frac{AB}{AC} = 1$$



(: D is the mid-point of BC, : BD = DC)

$$\Rightarrow$$
 AB = AC

Hence, $\triangle ABC$ is an isosceles.

So, Assertion (A) is true.

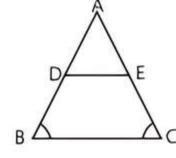
Reason (R): It is also true.

Hence, both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).

28. (d) Assertion (A): In $\triangle ABC$, we have $\angle B = \angle C$

$$\Rightarrow$$
 AC = AB

(: Sides opposite to equal angles are equal)



$$\Rightarrow AE + EC = AD + DB$$

$$\Rightarrow AE + CE = AD + DB$$

$$\Rightarrow AE + CE = AD + CE$$

$$\Rightarrow AE + CE = AD + CE$$

$$\Rightarrow AE = AD$$

$$(BD = CE (Given))$$

Thus, we have

and
$$AD = AE$$

$$BD = CE$$

$$\frac{AD}{BD} = \frac{AE}{CE} \implies \frac{AD}{DB} = \frac{AE}{EC}$$

 \Rightarrow DE II BC

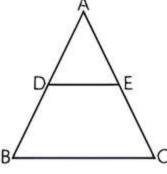
So, Assertion (A) is false.

Reason (R): It is true statement.

Hence, Assertion (A) is false but Reason (R) is true.

29. (d) Assertion (A): We have.

$$\frac{AD}{DB} = \frac{AE}{EC}$$
 [::DE || BC]
$$\Rightarrow \frac{7x - 4}{3x + 4} = \frac{5x - 2}{3x}$$



$$\Rightarrow$$
 $21x^2 - 12x = 15x^2 + 20x - 6x - 8$

$$\Rightarrow 6x^2 - 26x + 8 = 0$$

$$\Rightarrow$$
 3x² - 13x + 4 = 0

TR!CK-

Product of extreme terms = $3 \times 4 = 12$

$$12 = 6 \times 2 = 3 \times 4 = 12 \times 1$$

Here, we will take 12 and 1 as a factors of 12. So, middle term

$$-13 = -12 - 1$$

$$\Rightarrow 3x^2 - 12x - x + 4 = 0$$

$$\Rightarrow$$
 $3x(x-4)-1(x-4)=0$

$$\Rightarrow (x-4)(3x-1)=0$$

$$\Rightarrow \qquad x = 4, \frac{1}{3}$$

So. Assertion (A) is false.

Reason (R): It is true statement.

Hence, Assertion (A) is false but Reason (R) is true.

- **30.** Proportional
- **31**. In ΔABC and ΔDEF,

$$\angle B = \angle E$$
 (Given)

$$\angle C = \angle F$$
 (Given)

32. In ΔDEF and ΔQRP.

$$\angle D = \angle Q$$
 (Given)

$$\angle E = \angle R$$
 (Given)

ΔDEF ~ ΔQRP (By AA similarity)



$$\frac{DE}{QR} = \frac{DF}{QP} = \frac{EF}{RP}$$

- 33. Parallel
- 34. Congruent
- **35**. True
- **36**. True
- **37**. True

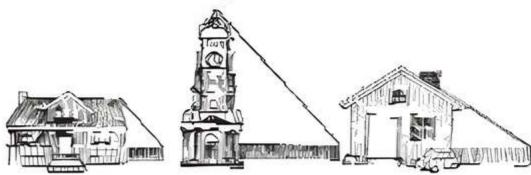


Case Study Based Questions >

Case Study 1

Digvijay is trying to find the average height of a tower near his house. He is using the properties of similar triangles. The height of Digvijay's house is 20 m when Digvijay's house casts a shadow 10 m long on the ground.

At the same time, the tower casts a shadow 50 m long on the ground and the house of Anshul casts 20 m shadow on the ground.



Based on the above information, solve the following questions:

- Q 1. The height of the tower is:
 - a. 10 m
- b. 20 m
- c. 50 m
- d. 100 m
- Q 2. When Digvijay's house casts a shadow of 18 cm, the length of the shadow of the tower is:
 - a. 18 m
- b. 20 m
- c. 90 m
- d. 100 m
- Q 3. The height of Anshul's house is:
 - a. 20 m
- b. 40 m
- c. 50 m
- d. 100 m
- Q 4. When the tower casts a shadow of 40 m, same time the length of the shadow of Anshul's house is:
 - a. 16 m
- h /10 m
- c. 100 m
- d. None of these
- Q 5. Which of the following similarity criterion does not exist?
 - a. AA
- b. SAS
- c. SSS
- d. RHS

Solutions

Let CD = h m be the height of the tower.
 Let BE = 20 m be the height of Digvijay house and GF be the height of Anshul's house.

$$\frac{AC}{AB} = \frac{CD}{EB}$$

 \Rightarrow

 $\frac{50}{10} = \frac{h}{20}$

 $h = 100 \, \text{m}$

So, option (d) is correct.

2. Given AB = 18 m, let AC = x
In similar ΔABE and ΔACD

$$\frac{AB}{AC} = \frac{BE}{CD}$$
 \Rightarrow $\frac{18}{x} = \frac{20}{100}$

$$\Rightarrow x = \frac{18 \times 100}{20} = 18 \times 5 = 90 \text{ m}$$

So. option (c) is correct.

3. Let height of Anshul's house be $GF = h_1$ Since. $\Delta HFG \sim \Delta HCD$

$$\therefore \quad \frac{HF}{HC} = \frac{FG}{CD} \quad \Rightarrow \quad \frac{20}{50} = \frac{h_1}{100}$$

HC CD 50 10
$$h_1 = \frac{20 \times 100}{50} = 40 \,\text{m}$$

So, option (b) is correct.

4. Given. HC = 40 cm

Let length of the shadow of Anshul's house be HF = l m.

Since. ΔHFG ~ ΔHCD

$$\frac{HF}{HC} = \frac{FG}{CD}$$

$$\Rightarrow \qquad \frac{l}{40} = \frac{40}{100}$$

$$\Rightarrow \qquad l = \frac{40 \times 40}{100} = 16 \,\mathrm{m}$$

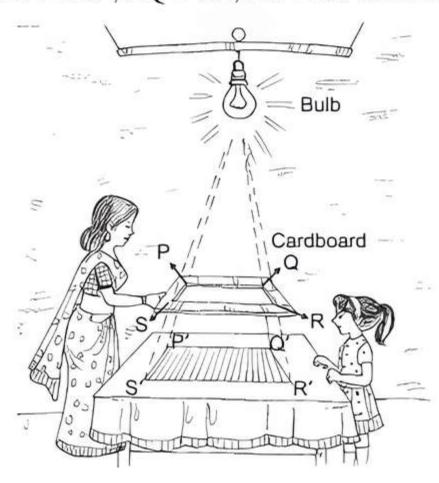
So. option (a) is correct.

RHS similarity Criterion does not exist.

So, option (d) is correct.

Case Study 2

Gaurav placed a light bulb at a point O on the ceiling and directly below it placed a table. He cuts a polygon, say a quadrilateral PQRS, from a plane cardboard and place this cardboard parallel to the ground between the lighted bulb and the table. Then a shadow of PQRS is cast on the table as P'Q'R'S'. Quadrilateral P'Q'R'S' is an enlargement of the quadrilateral PQRS with scale factor 1:3. Given that PQ = 2.5 cm, QR = 3.5 cm. RS = 3.4 cm and PS = 3.1 cm; $\angle P = 115^{\circ}$, $\angle Q = 95^{\circ}$, $\angle R = 65^{\circ}$ and $\angle S = 85^{\circ}$.



Based on the given information, solve the following questions:

Q1. The length of R'S' is:

a. 3.4 cm

b. 10.2 cm c. 6.8 cm

d. 9.5 cm

Q 2. The ratio of sides P'Q' and Q'R' is:

a. 5:7

b. 7:5

c. 7:2

d. 2:7

Q 3. The measurement of $\angle Q'$ is:

a. 115°

b. 95°

c. 65°

d. 85°

Q 4. The sum of the lengths Q'R' and P'S' is:

a. 12.3 cm

b. 6.7 cm

c. 19.8 cm

d. 9 cm

Q 5. The sum of angles of quadrilateral P'Q'R'S' is:

a. 180°

b. 270°

c. 300°

d. 360°

Solutions

1. Given, scale factor is 1:3.

$$R'S' = 3 \times 3.4 = 10.2 \text{ cm}$$

So. option (b) is correct.

2. Since, P'Q' = $3 PQ = 3 \times 2.5 = 7.5 cm$

and
$$Q'R' = 3 QR = 3 \times 3.5 = 10.5 cm$$

$$\frac{P'Q'}{Q'R'} = \frac{7.5}{10.5} = \frac{5}{7}$$
 or 5:7

So, option (a) is correct.

3. Quadrilateral P'Q'R'S' is similar to PQRS

So, option (b) is correct.

4. $Q'R' = 3 QR = 3 \times 3.5 = 10.5 cm$

and P'S' =
$$3 PS = 3 \times 3.1 = 9.3 cm$$

$$\therefore$$
 Q'R' + P'S' = 10.5 + 9.3 = 19.8 cm

So, option (c) is correct.

5. Since, PQRS ~ P'Q'R'S'

$$\therefore \qquad \angle P' = \angle P = 115^{\circ}$$

$$\angle Q' = \angle Q = 95^{\circ}$$

$$\angle R' = \angle R = 65^{\circ}$$

and
$$\angle S' = \angle S = 85^{\circ}$$

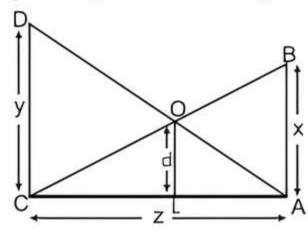
$$\angle P' + \angle Q' + \angle R' + \angle S' = 115^{\circ} + 95^{\circ} + 65^{\circ} + 85^{\circ}$$
$$= 360^{\circ}$$

i.e., the sum of angles of quadrilateral P'Q'R'S' is 360°.

So, option (d) is correct.

Case Study 3

Anika is studying in class X. She observe two poles DC and BA. The heights of these poles are x m and y m respectively as shown in figure:



These poles are z m apart and O is the point of intersection of the lines joining the top of each pole to the foot of opposite pole and the distance between point O and L is d. Few questions came to his mind while observing the poles.

Based on the above information, solve the following questions:

- Q 1. Which similarity criteria is applicable in \triangle CAB and \triangle CLO?
- Q 2. If x = y, prove that BC : DA = 1 : 1.
- Q 3. If CL = a, then find a in terms of x, y and d.

OR

If AL = b, then find b in terms of x, y and d.

Solutions

1. In $\triangle CAB$ and $\triangle CLO$, we have

(common)

... By AA similarity criterion,

2. In ΔDCA and ΔBAC,

$$DC = BA$$

BA
$$(:: x = y \text{ (Given)})$$

$$\angle DCA = \angle BAC$$

CA = AC

(Each 90°) (Common)

By SAS similarity criterian.

$$\frac{DA}{BC} = \frac{DC}{BA} = \frac{y}{x}$$

$$\frac{BC}{DA} = \frac{x}{y} = \frac{x}{x} = \frac{1}{1}$$

BC: DA ∞ 1:1

proved.

TiF

Corresponding sides of similar triangles are proportional.

$$\frac{CA}{CL} = \frac{AB}{LO} \implies \frac{z}{a} = \frac{x}{d} \implies a = \frac{zd}{x}$$

In ΔALO and ΔACD,

We have

$$\angle ALO = \angle ACD = 90^{\circ}$$

$$\angle A = \angle A$$

(common)

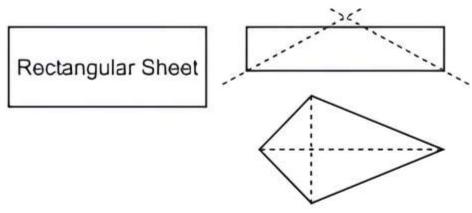
.. By AA similarity criterion.

$$\therefore \frac{AL}{AC} = \frac{OL}{DC} \implies \frac{b}{z} = \frac{d}{y} \implies b = \frac{zd}{y}$$

Case Study 4

Before Basant Panchami, Samarth is trying to make kites at home. So, he take a rectangular sheet and fold it horizontally, then vertically and fold it transversally. After cutting transversally, he gets a kite shaped figure as shown below:





Based on the above information, solve the following questions:

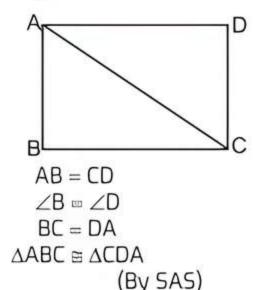
- Q1. What is the angle between diagonals of a rectangle?
- Q 2. Prove that two triangles divided by a diagonal in rectangle are similar as well as congruent.
- Q 3. Prove that the longest diagonal of a kite bisect a pair of opposite angle.

OR

By which similarity criterion the triangles formed by longest diagonal in a kite are similar?

Solutions

- 1. Diagonals of a rectangle can bisect each other at any angle.
- 2. In AABC and ACDA



When two triangles are congruent, then they are similar also.

3. In ΔAOB and ΔAOD,

AB = AD

$$OA = OA \text{ (common)}$$
 $BO = DO$

(diagonal AC bisect the other B

diagonal BD)

 $\triangle AOB \sim \triangle AOD$

(by SSS similarity)

 $\Rightarrow \triangle BAO = \angle DAO \dots (1)$

In $\triangle BOC$ and $\triangle DOC$.

 $BC = DC$
 $OC = OC \text{ (common)}$

BO - OD (Diagonal AC bisect the other diagonal BD) (by SSS similarity) ΔBOC ~ ΔDOC .

 $\angle BCO = \angle DCO$...(2) From (1) and (2), It is clear that, the longest diagonal

of a kite bisect a pair of opposite angle.

ΔABC ~ ΔADC

In
$$\triangle$$
ABC and \triangle ADC,
AB = AD
BC = DC
AC = AC

(common)

(by SSS criterion)

In $\triangle ABC$ and $\triangle ADC$. AB = AD $\angle ABC = \angle ADC$ BC = DCΔABC ~ ΔADC

(by SAS criterion)

In $\triangle ABC$ and $\triangle ADC$.

$$\angle BAC = \angle DAC$$

(
$$:: \angle BAO = \angle BAC. \angle DAO = \angle DAC.$$
 proved above)

$$\angle BCA = \angle DCA$$

So. required similarity criterions are SSS. SAS and AAA.

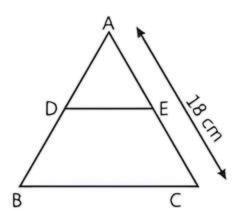


Very Short Answer Type Questions >

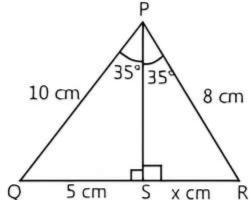
Q1. In $\triangle PQR$, S and T are points on the sides PQ and PR respectively, such that ST || QR. If PS = 4 cm, PQ = 9 cm and PR = 4.5 cm, then find PT.

[CBSE 2015, 16, 17]

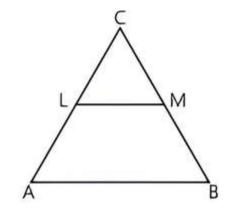
- Q 2. In two triangles ABC and DEF, if $\angle A = \angle E$ and $\angle B = \angle F$. Then, prove that $\frac{AB}{AC} = \frac{B}{ED}$.
- Q 3. In the given figure, DE is parallel to BC. If $\frac{AD}{DB} = \frac{2}{3}$ and AC = 18 cm, then find AE.



Q 4. Find the value of x in the given figure.



- Q 5. If the corresponding medians of two similar triangles are in the ratio 5: 7, then find the ratio of their corresponding sides. [CBSE 2015]
- Q 6. In the given figure, LM || AB. If AL = x 3, AC = 2x, BM = x - 2 and BC = 2x + 3, find the value of x.

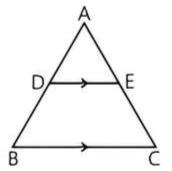




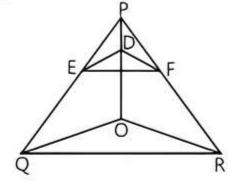


Short Answer Type-I Questions >

Q 1. In the given figure, a \triangle ABC, DE || BC, so that AD = (4x-3) cm, AE = (8x-7) cm, BD = (3x-1) cm and CE = (5x-3) cm. Find the value of x. [CBSE 2015]

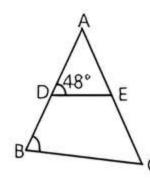


Q 2. In the following figure, DE || OQ and DF || OR, show that EF || QR. [NCERT EXERCISE]



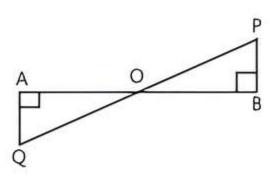
- Q 3. X and Y are points on the sides AB and AC respectively of a triangle ABC, such that $\frac{AX}{AB} = \frac{1}{4}$, AY = 2 cm and YC = 6 cm. Find whether XY || BC or
 - AY = 2 cm and YC = 6 cm. Find whether XY || BC or not. [CBSE 2015]
- Q 4. In figure, if AD = 6cm, DB = 9cm, AE = 8cm and EC = 12cm and \angle ADE = 48°. Find \angle ABC.

[CBSE SQP 2023-24]

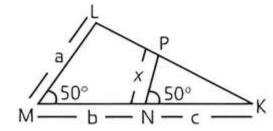


Q 5. In the given figure, QA \perp AB and PB \perp AB. If AO = 20 cm, BO = 12 cm, PB = 18 cm, find AQ.

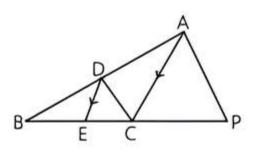
[CBSE 2017]



Q 6. In the given figure, $\angle M = \angle N = 50^{\circ}$. Express x in terms of a, b and c where a, b and c are the lengths of LM, MN and NK respectively.



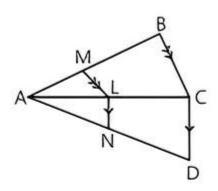
- Q 7. A vertical stick which is 15 cm long casts a 12 cm long shadow on ground. At the same time, a vertical tower casts a 50 m long shadow on the ground. Find the height of the tower. [CBSE 2016]
- Q 8. In the given figure, DE || AC and $\frac{BE}{EC} = \frac{BC}{CP}$. Prove that DC || AP.



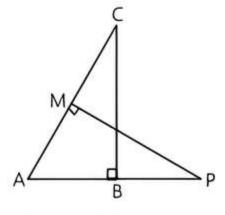
Q 9. In the given figure, LM || CB and LN || CD. Prove that

$$\frac{AM}{AN} = \frac{AB}{AD}$$

[CBSE 2023, NCERT EXERCISE]

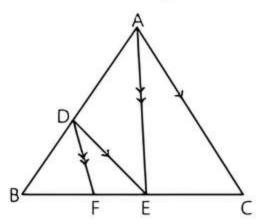


Q 10. In the given figure, ABC and AMP are two right triangles, right angled at B and M, respectively. Prove that \triangle ABC ~ \triangle AMP. [CBSE 2023]



Q 11. In the given figure, DE || AC and DF || AE.

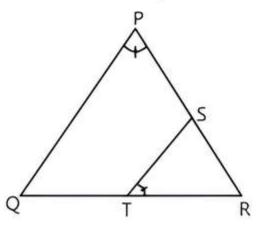
[CBSE 2023, NCERT EXERCISE]



Prove that $\frac{BE}{FE} = \frac{BE}{FC}$.

- Q 12. ABCD is a trapezium such that BC||AD and AB = 4 cm. If the diagonals AC and BD intersect at O such that $\frac{AO}{OC} = \frac{OB}{OD} = \frac{1}{2}$, then find CD.
- Q 13. S and T are points on sides PR and QR of \triangle PQR such that \angle P = \angle RTS. Show that \triangle RPQ ~ \triangle RTS.

[CBSE 2023, NCERT EXERCISE]

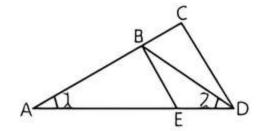


Q 14. The diagonal BD of a quadrilateral ABCD bisects both $\angle B$ and $\angle D$. Show that $\frac{AB}{BC} = \frac{AD}{CD}$.

Q 15. In the given figure below, $\frac{AD}{AE} = \frac{AC}{BD}$ and $\angle 1 = \angle 2$.

Show that $\triangle BAE \sim \triangle CAD$.

[CBSE SQP 2022-23]

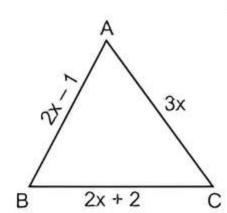


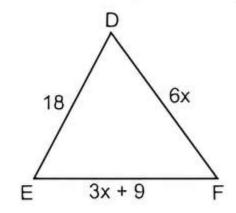


Short Answer Type-II Questions >

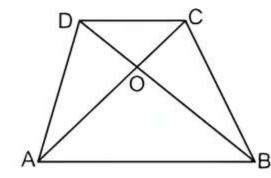
Q 1. In the given figure, if \triangle ABC \sim \triangle DEF and their sides of lengths (in cm) are marked along them, then find the lengths of sides of each triangle.

[NCERT EXEMPLAR; CBSE 2020]

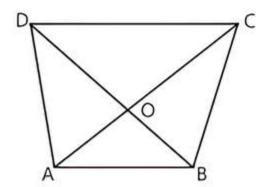




Q 2. Diagonals AC and BD of trapezium ABCD with AB || DC intersect each other at point O. Show that [CBSE 2023, NCERT EXERCISE]



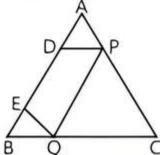
Q 3. The diagonals of a quadrilateral ABCD intersect each other at the point O such that $\frac{AO}{BO} = \frac{CO}{OD}$.



Show that quadrilateral ABCD is a trapezium.

[CBSE 2023, NCERT EXERCISE]

Q 4. In the given figure, D and E are two points lying on side AB, such that AD = BE. If DP || BC and EQ || AC, then prove that PQ | AB.

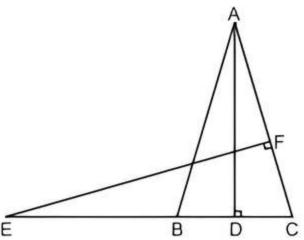


Q 5. If AD and PM are medians of triangles ABC and PQR, respectively, where \triangle ABC \sim \triangle PQR, prove that

$$\frac{AB}{PO} = \frac{AD}{PM}$$

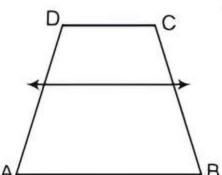
[NCERT EXERCISE; CBSE 2017]

Q 6. In the given figure, E is a point on the side CB produced of an isosceles triangle ABC with AB = AC. If AD \perp BC and EF \perp AC, then prove that \triangle ABD \sim \triangle ECF. [NCERT EXERCISE, CBSE 2023]



Q7. In the given figure, if ABCD is a trapezium in which AB || CD || EF, then prove that

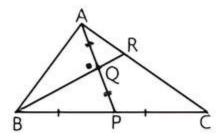
[CBSE SQP 2023-24]





Long Answer Type Questions >

Q 1. In the given figure of \triangle ABC, P is the mid-point of BC and Q is the mid-point of AP. If extended BQ meets AC in R, prove that $AR = \frac{1}{3}CA$.

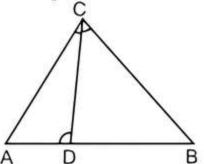


Q 2. ABCD is a parallelogram, P is a point on side BC and DP when produced meets AB produced at L. Prove that:

(i)
$$\frac{DP}{PL} = \frac{DC}{BL}$$

(i)
$$\frac{DP}{PL} = \frac{DC}{BL}$$
 (ii) $\frac{DL}{DP} = \frac{AL}{DC}$

Q 3. In the given figure, $\angle ADC = \angle BCA$; prove that \triangle ACB $\sim \triangle$ ADC. Hence find BD if AC = 8 cm and AD = 3 cm. [NCERT EXEMPLAR, CBSE SQP 2023-24]



Q 4. Prove that if a lines is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, the other two sides are divided in the same ratio.

In $\triangle PQR$, S and T are points on PQ and PR respectively. $\frac{PS}{SQ} = \frac{PT}{TR}$ and $\angle PST = \angle PRQ$. Prove

that PQR is an isosceles triangle. [CBSE SQP 2023-24] OR

If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, then prove that the other two sides are divided in the same ratio. [CBSE 2023]

Solutions

Very Short Answer Type Questions

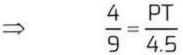
1. Given, PS = 4 cm, PQ = 9 cm and PR = 4.5 cm



If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, then the other two sides are divided in the same ratio.

Since. ST II QR. then by BPT. we have





or
$$PT = \frac{4 \times 4.5}{9} = 2 \text{ cm}$$

PT = 2 cm. Hence.

2. In ΔABC and ΔEFD,

$$\angle A = \angle E$$
 and $\angle B = \angle F$

(Given)

ΔABC ~ ΔEFD

(By AA similarity criterion)

$$\frac{AB}{EF} = \frac{AC}{ED} \Rightarrow \frac{AB}{AC} = \frac{EF}{ED}$$

Hence proved.

3. In AABC, DE || BC.

$$\frac{AD}{DR} = \frac{A}{F}$$

(By Thales theorem)

$$\Rightarrow \frac{2}{3} = \frac{AE}{EC} \Rightarrow \frac{3}{2} = \frac{EC}{AE}$$

$$\Rightarrow \frac{1}{2}$$

Adding 1 on both the sides, we get

$$\frac{3}{2} + 1 = \frac{EC}{AE} + 1 \implies \frac{3+2}{2} = \frac{EC + AE}{AE}$$

$$\Rightarrow \frac{5}{2} = \frac{AC}{AE}$$

$$\frac{5}{2} = \frac{AC}{AE}$$
 \Rightarrow $\frac{5}{2} = \frac{18}{AE}$

$$\Rightarrow$$

$$5AE = 36$$

$$\Rightarrow$$

$$AE = \frac{36}{5} \Rightarrow AE = 7.2 \text{ cm}$$

In ΔPSQ and ΔPSR,

$$\angle$$
QSP = \angle RSP = 90°

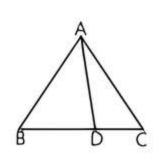
(By AA similarity)

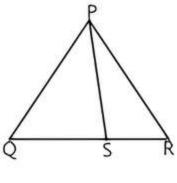
$$\frac{PQ}{PR} = \frac{SQ}{SR}$$

$$\Rightarrow$$

$$\frac{10}{8} = \frac{5}{x} \Rightarrow x = 4 \text{ cm}$$

5. Let ABC and PQR are two similar triangles with medians AD and PS respectively.





Then.

$$\frac{AD}{PS} = \frac{5}{7}$$

(Given)

TR!CK-

The ratio of the medians of two similar triangles is equal to the ratio of their corresponding sides.

$$\Rightarrow \frac{AB}{PQ} = \frac{AD}{PS} = \frac{5}{7}$$

Hence, the ratio of corresponding sides is 5 : 7.

6.

If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, then the other two sides are divided in the same ratio.

In AABC, LM | AB

$$\frac{AL}{LC} = \frac{BM}{MC}$$

$$\Rightarrow \frac{AL}{AC - AL} = \frac{BM}{BC - BM}$$

$$\Rightarrow \frac{x-3}{2x-(x-3)} = \frac{x-2}{(2x+3)-(x-2)} \Rightarrow \frac{x-3}{x+3} = \frac{x-2}{x+5}$$

$$\Rightarrow$$
 $(x-3)(x+5)=(x-2)(x+3)$

$$\Rightarrow x^2 + 2x - 15 = x^2 + x - 6$$

Short Answer Type-I Questions

1. In \triangle ABC, DE II BC, so by BPT.

$$\frac{AD}{BD} = \frac{AE}{CE} \implies \frac{4x-3}{3x-1} = \frac{8x-7}{5x-3}$$

$$\Rightarrow$$
 $(4x-3)(5x-3)=(8x-7)(3x-1)$

$$\Rightarrow 20x^{2} - 12x - 15x + 9 = 24x^{2} - 8x - 21x + 7$$

$$\Rightarrow 24x^{2} - 20x^{2} - 29x + 27x + 7 - 9 = 0$$

$$\Rightarrow 24x^2 - 20x^2 - 29x + 27x + 7 - 9 = 0$$

$$\Rightarrow 4x^2 - 2x - 2 = 0$$

$2(2x^2-x-1)=0$

TR!CK

$$2 = 2 \times 1$$

:. Here, we have taken 2 and 1 as a factors of 2. So, middle term, -1 = 1 - 2.

$$\Rightarrow 2x^2 - 2x + x - 1 = 0$$

$$\Rightarrow 2x(x-1)+1(x-1)=0$$

$$\Rightarrow$$
 $(x-1)(2x+1)=0$



$$\Rightarrow x-1=0 \text{ and } 2x+1=0$$

$$\Rightarrow x=1 \text{ and } x=-\frac{1}{2}$$

 $\frac{1}{2}$, then AD. BD. AE and CE all are

negative.

$$\therefore \quad x \neq -\frac{1}{2}$$

Hence, the value of x is 1.

COMMON ERR(!)R

Sometimes students take both value of x as a answer but it is wrong. Students should cross check the value of x.

2.



If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, then the other two sides are divided in the same ratio.

In
$$\Delta$$
 POQ. DE II OQ

$$\frac{PE}{EQ} = \frac{PD}{DO}$$

(By BPT) ...(1)

In Δ POR, DF || OR

$$\frac{PF}{FR} = \frac{PD}{DO}$$

(By BPT) _..(2)

$$\frac{PE}{EQ} = \frac{PF}{FR}$$

If a line divides any two sides of a triangle in the same ratio, then the line is parallel to the third side.

Hence proved.

2 cm

6 cm

3. Given.
$$\frac{AX}{AB} = \frac{1}{4}$$

$$\therefore$$
 XB = AB - AX = 4 $k - k = 3k$

$$\frac{AX}{XB} = \frac{k}{3k} = \frac{1}{3}$$

and

$$\frac{AY}{YC} = \frac{2}{6} = \frac{1}{3}$$

TR!CK-

If a line divides any two sides of a triangle in the same ratio, then the line is parallel to the third side.

$$\frac{AX}{XB} = \frac{AY}{YC}$$

XY || BC Hence.

(By converse of BPT)

4. Given, AD = 6cm,

DB = 9cm, AE = 8cm.

 $EC = 12cm \text{ and } \angle ADE = 48^{\circ}$

Here.
$$\frac{AD}{DD} = \frac{6}{D} = \frac{2}{3}$$

and
$$\frac{AE}{EC} = \frac{8}{12}$$

$$\frac{AD}{DB} = \frac{AE}{EC}$$

.. DE II BC (By Converse of BPT)

In AABC, DEIIBC

(Corresponding angles)

5. In ΔOAQ and ΔOBP.

$$\Rightarrow$$
 $\frac{AO}{BO} = \frac{AQ}{PB}$ (Corresponding sides are proportional)

$$\Rightarrow \frac{20}{12} = \frac{AQ}{18}$$

$$\Rightarrow AQ = \frac{18 \times 20}{12} = 30 \text{ cm}$$

6. Given,
$$LM = a$$
, $PN = x$, $MN = b$ and $NK = c$

In \triangle PNK and \triangle LMK,

$$\angle$$
 PNK = \angle LMK (Each 50°)

$$\angle$$
 PKN = \angle LKM
 \triangle PNK ~ \triangle LMK

(Common angle) (By AA similarity)

So.
$$\frac{NK}{MK} = \frac{PN}{LM}$$

(Corresponding sldes are proportional)

$$\Rightarrow \frac{NK}{MN + NK} = \frac{PN}{LM}$$

$$\Rightarrow \frac{c}{b+c} = \frac{x}{a} \quad \text{or} \quad x = \frac{ac}{b+c}$$

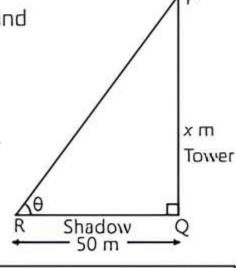
7. Let AB be the vertical stick and BC be its shadow.

Given. AB = 15 cm = 0.15 m

BC = 12 cm = 0.12 mand

Let PQ be the vertical tower and QR be its shadow.

In \triangle ABC and \triangle PQR.



...

Two triangles are similar, if their corresponding sides are in proportional.

$$\angle$$
 ABC = \angle PQR

(Each 90°)

(Stick)

0.15 m

$$\angle$$
 ACB = \angle PRQ

(Angular elevation of the sun at the same time)

(By AA similarity)

 $0.12 \, \mathrm{m}$

(Shadow)

So.
$$\frac{AB}{PQ} = \frac{BC}{QR}$$

(Corresponding sides are proportional)

$$\Rightarrow \frac{0.15}{x} = \frac{0.12}{50}$$

$$\Rightarrow \qquad x = \frac{0.15 \times 50}{0.12}$$

 $x = 62.5 \, \text{m}$

or

Hence, the height of the tower is 62.5 m.

B. In ΔABC

Given that, DE II AC

$$\therefore \quad \frac{BE}{EC} = \frac{BD}{DA} \qquad (By BPT) \qquad \dots (1)$$

But
$$\frac{BE}{EC} = \frac{BC}{CP}$$
 (given) ... (2)

from eqs. (1) and (2), we get $\frac{BD}{DA} = \frac{BC}{CP}$

 \Rightarrow DC || AP. (By converse of BPT) Hence proved.

Given: Line segment LM || CB and LN || CD.

To Prove:
$$\frac{AM}{AN} = \frac{AB}{AD}$$

Proof: In $\triangle ABC$, M is a point on side AB and L is a point on side AC from which line segment LM IICB.

$$\frac{AM}{MB} = \frac{AL}{LC}$$

[From BPT]

$$\Rightarrow \frac{MB}{AM} = \frac{LC}{AL}$$

(Taking reciprocals)

$$1 + \frac{MB}{AM} = 1 + \frac{LC}{AL}$$

(Adding 1 on both sides)

$$\Rightarrow \frac{AM + MB}{AM} = \frac{AL + LC}{AL}$$

$$\frac{AB}{AM} = \frac{AC}{AL} \quad [\because AB = AM + MB, AC = AL + LC]$$

Similarly, In AACD, LN || CD

$$\frac{AN}{ND} = \frac{AL}{LC}$$

(From BPT)

$$\Rightarrow \frac{ND}{AN} = \frac{LC}{AL}$$

(Taking reciprocals)

$$\Rightarrow 1 + \frac{ND}{AN} = 1 + \frac{LC}{AL}$$

$$\Rightarrow \frac{AN + ND}{AN} = \frac{AL + LC}{AL}$$

$$\Rightarrow \frac{AD}{AN} = \frac{AC}{AL} \left(:: AD = AN + ND, AC = AL + LC \right)$$
...(2)

From eqs (1) and (2), we get

$$\frac{AB}{AM} = \frac{AD}{AN}$$

$$\Rightarrow \frac{AM}{AB} = \frac{AN}{AD}$$

(Taking reciprocals)

$$\Rightarrow \frac{AM}{AN} = \frac{AB}{AD}$$

Hence proved.

10. Given: ABC and AMP are two right triangles, right angled at B and M, respectively.

Prove that: $\triangle ABC \sim \triangle AMP$

Proof: In \triangle ABC and \triangle AMP,

(Each 90°) $\angle ABC = \angle AMP$

 $\angle CAB = \angle PAM$

(Common angle)

∠ACB ··· ∠APM

(Same itself)

∴ ∆ABC ~ ∆AMP

(By AAA similarity criterion)

Hence proved

11. Given: In ΔABC, D is a point on side AB and two points E and F on the side BC. Line segments DF, DE and AE are drawn. DE || AC and DF || AE.

Prove that : $\frac{BF}{FE} = \frac{BE}{EC}$

Proof: ·· In ∆ABE, DF || AE

$$\frac{BF}{FF} = \frac{BD}{DA}$$

..... (1) (By BPT)

and In ∆ABC, DE ||AC

$$\frac{BE}{EC} = \frac{BD}{DA}$$

...(2) (By BPT)

From eqs. (1) and (2), we get

$$\frac{BF}{FF} = \frac{BE}{FC}$$

Hence proved.

12. In



When two non-parallel rays intersect at a point the angles formed between these rays at point of intersection in opposite directions are called vertically opposite angle.

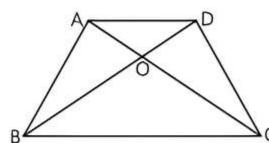
In $\triangle AOB$ and $\triangle COD$, we have

$$\angle AOB = \angle COD$$

(Vertically opposite angles)

$$\frac{AO}{OC} = \frac{OB}{OD} = \frac{1}{2}$$

(Given)



ΔAOB ~ ΔCOD (By SAS similarity criterion)

$$\therefore \quad \frac{AB}{CD} = \frac{AO}{OC} \Rightarrow \frac{4}{CD} = \frac{1}{2} \Rightarrow CD = B \text{ cm}$$

13. Given: In the given figure.

$$\angle P = \angle RTS$$

To Prove : △ RPQ ~ △ RTS Proof: In △ RPQ and △ RTS

$$\angle P = \angle RTS$$

(Given)

$$\angle P = \angle RTS$$

 $\angle R = \angle SRT$

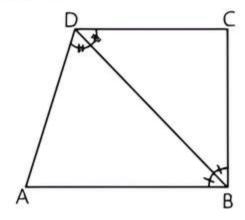
(common angle)

$$\angle Q = \angle RST$$

(some itself)

(By AAA similarity criterion) Hence proved.

14. Given: Diagonal BD of a quadrilateral ABCD bisects both $\angle B$ and $\angle D$.



To Prove: $\frac{AB}{BC} = \frac{AD}{CD}$

Proof: In $\triangle ABD$ and $\triangle CBD$

$$\angle ABD = \angle CBD$$

(∴ BD blsects ∠B)

$$BD = BD$$

(Common side)

(∴ BD bisects ∠D)

Thus, ΔABD ~ ΔCBD

(By ASA similarity criterion)

$$\therefore \frac{AB}{CB} = \frac{AD}{CD} \text{ or } \frac{AB}{BC} = \frac{AD}{CD}$$

Hence proved.

15. In ∆ABD.

$$\angle 1 = \angle 2$$

(Given)

BD = AB (Sides opposite to equal

angles are equal) ...(1)

Given,

$$\frac{AD}{AE} = \frac{AC}{BD}$$

Using eq. (1).

$$\frac{AD}{AE} = \frac{AC}{AB} \qquad ...(2)$$

In ΔBAE and ΔCAD.

$$\frac{AC}{AB} = \frac{AD}{AE}$$

(From eq. (2))

$$\angle A = \angle A$$

(Common)

(By SAS similarity criterion)

Hence proved.

Short Answer Type-II Questions

 Since. ΔABC ~ ΔDEF, so ratio of their corresponding sides is equal.

$$\frac{AB}{DE} = \frac{BC}{EE} = \frac{AC}{DE}$$

$$\Rightarrow$$

$$\frac{2x-1}{18} = \frac{2x+2}{3x+9} = \frac{3x}{6x}$$

$$\Rightarrow$$

$$\frac{2x-1}{18} = \frac{2x+2}{3x+9} = \frac{1}{2}$$

Taking first and third parts, we get

$$\frac{2x-1}{18} = \frac{1}{2}$$

$$\supset$$

$$2x = 9 + 1$$

$$\Rightarrow$$

$$x = \frac{9+1}{2} = \frac{10}{2} = 5$$

∴ Sides of ∆ABC,

$$AB = (2x - 1) = 2 \times 5 - 1 = 10 - 1 = 9 \text{ cm}.$$

$$BC = 2x + 2 = 2 \times 5 + 2 = 10 + 2 = 12 \text{ cm}$$

and

$$AC = 3x = 3 \times 5 = 15 \text{ cm}$$

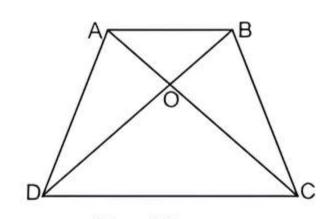
∴ Sides of ∆DEF.

$$EF = 3 \times 5 + 9 = 15 + 9 = 24 \text{ cm}$$

and

$$DF = 6x = 6 \times 5 = 30 \text{ cm}$$

Given: ABCD is a trapezium in which ABIICD and its diagonals AC and BD Intersect at point O.



To Prove:

$$\frac{OA}{OC} = \frac{OB}{OD}$$

Proof: .. ABIICD and AC is a transversal.

∠0AB == ∠0CD

(alternate angles)

and

$$\angle AOB = \angle COD$$

(vertically opposite angles)

Now. In $\triangle AOB$ and $\triangle OCD$.

From AA similarity.

$$\frac{OA}{OC} = \frac{OB}{OD}$$
 (From the proportionality of side)

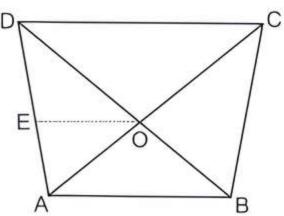
Hence proved.

3. Given: In a quadrilateral ABCD, $\frac{AO}{BO} = \frac{CO}{DO}$

To Prove: ABCD is a trapezium.

Construction: Let us draw a quadrilateral ABCD.

Draw a line OE || AB.



Proof: In ∆ ABD. OE || AB



If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, then the other two sides are divided in the same ratio.

By using basic proportionality theorem, we get

$$\frac{AE}{ED} = \frac{BO}{OD} \qquad ...(1)$$

But, it is given that

$$\frac{AO}{BO} = \frac{CO}{DO}$$

$$\frac{AO}{OC} = \frac{BO}{OD}$$

From eqs. (1) and (2), we get

$$\frac{AE}{ED} = \frac{AO}{OC}$$

TR!CK

If a line divides any two sides of a triangle in the same ratio, then the line is parallel to the third side.





EO II DC \Rightarrow

(By the converse of basic proportionality theorem)

AB II OE II DC

AB || DC

ABCD is a trapezium.

Hence proved.

4. Given: AD = BE, DP || BC and EQ || AC

To Prove: PQ | AB



If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, then the other two sides are divided in the same ratio.

Proof: In \triangle ABC. by BPT we have

$$\frac{AD}{DB} = \frac{AP}{PC}$$

(:: DP || BC) ...(1)

Again, in Δ ABC, by BPT we have

$$\frac{BE}{EA} = \frac{BQ}{QC}$$

(: EQ II AC)

Or

$$\frac{AD}{DB} = \frac{BQ}{OC}$$

...(2)

(:
$$AD = BE$$
 and $EA = ED + DA = ED + BE = DB)$

TR!CK-

If a line divides any two sides of a triangle in the same ratio, then the line is parallel to the third side.

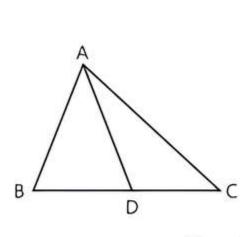
From eqs. (1) and (2), we get

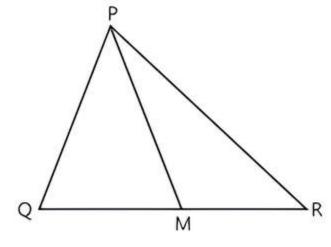
$$\frac{AP}{PC} = \frac{BQ}{QC}$$

In AABC. P and Q divide the sides CA and CB respectively in the same ratio.

Hence proved.

5. Given: ΔABC ~ ΔPQR





To Prove: $\frac{AB}{PO} = \frac{AD}{PM}$

$$: \frac{AB}{PO} = \frac{AD}{PM}$$

Proof: Since, ΔABC ~ ΔPQR

$$\frac{AB}{PO} = \frac{AC}{PR} = \frac{BC}{OR} \qquad --(1)$$

(Corresponding sides are proportional)

Also,
$$\angle A = \angle P$$
, $\angle B = \angle Q$, $\angle C = \angle R$...(2)

(Corresponding angles are equal)

Since, AD and PM are medians, they will divide their opposite sides.

$$\therefore BD = \frac{BC}{2} \text{ and } QM = \frac{QR}{2}$$

...(3)

From eqs. (1) and (3), we get

$$\frac{AB}{PQ} = \frac{BD}{QM} \qquad ...(4)$$

Now, in \triangle ABD and \triangle PQM.

$$\angle B = \angle Q$$

(Using eq. (2))

$$\frac{AB}{BC} = \frac{BD}{CM}$$

(Using eq. (4))

$$\Delta$$
 ABD \sim Δ PQM

(By SAS similarity)

$$\frac{PQ}{AB} = \frac{QM}{BD} = \frac{BN}{AD}$$

(Corresponding sides are proportional)

Hence proved.

6. It is given that ABC is an isosceles triangle.

$$AB = AC$$

$$\angle ABD = \angle ECF$$

(:. Angles opposite to equal sides are equal)

In ΔABD and ΔECF

$$\angle ADB = \angle EFC$$

(Each 90°)

$$\angle \mathsf{ABD} = \angle \mathsf{ECF}$$

ΔABD ~ ΔECF

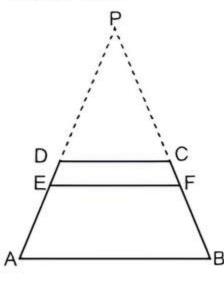
(Proved above) (By AA similarity) Proved.

7. Given: In the given figure, AB || CD || EF.

To Prove:
$$\frac{AE}{ED} = \frac{BF}{FC}$$

Construction: Produce AD and BC to meet at P (say).

Proof: In $\triangle PEF$, we have



DCIIEF

$$\frac{PD}{DE} = \frac{PC}{CE}$$

(By Thales theorem)

 $\frac{PD}{DE} + 1 = \frac{PC}{CE} + 1$

(Adding 1 on both sides)

$$\Rightarrow \frac{PD + DE}{DE} = \frac{PC + CF}{CF}$$

 $\frac{PE}{DF} = \frac{PF}{CF}$ (: PE = PD + DE, PF = PC + CF)

In $\triangle PAB$, we have

EF II AB

On dividing eq. (1) by eq. (2), we get

 $\frac{EA}{DE} = \frac{FB}{CF}$ \Rightarrow

or

Hence proved.

(By BPT) ...(2)

Long Answer Type Questions

1. Given: In AABC. P is the mid-point of BC and Q is the mid-point of AP.

To Prove: $RA = \frac{1}{3}CA$

Construction: Draw PT || BR. Proof: In Δ CBR, PT || BR



(By BPT)

...(2)



If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, then the other two sides are divided in the same ratio.

$$\Rightarrow \frac{CT}{TR} = 1$$

(∵ P is mid-point of BC *i.e.*, PB = CP)

In Δ APT, QR || PT

$$\frac{AQ}{QP} = \frac{AR}{RT}$$
 (By BPT)

$$\Rightarrow 1 = \frac{AR}{RT} (::Q \text{ is mid-point of AP } \text{Le., AQ = QP})$$

$$\Rightarrow$$
 AR $=$ RT
From eqs. (1) and (2), we get

$$AR = RT = CT$$

$$\therefore AR = \frac{1}{3}AC$$

$$AR = \frac{1}{3}AC$$
 Hence proved.

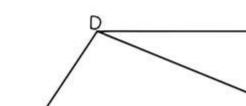
2. Given: A parallelogram ABCD in which P is a point on side BC such that DP produced meets AB produced at L

BPIIAD

To Prove: (i)
$$\frac{DP}{PL} = \frac{DC}{BL}$$

(ii)
$$\frac{DL}{DP} = \frac{AL}{DC}$$

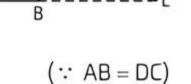
Proof: (i) In ∆ALD, we have



$$\Rightarrow \frac{BL}{AB} = \frac{PL}{DP}$$

 $\frac{LB}{BA} = \frac{LP}{PD}$

$$\Rightarrow \quad \frac{BL}{DC} = \frac{PL}{DP}$$



$$\Rightarrow \frac{1}{PL} = \frac{1}{BL}$$

(Taking reciprocals of both sides) Hence proved.

(ii) From part (i). we have

$$\frac{DP}{PL} = \frac{DC}{BL}$$

$$\Rightarrow \frac{PL}{DP} = \frac{BL}{DC}$$
 (Taking reciprocals of both sides)

$$\Rightarrow \frac{PL}{DP} = \frac{BL}{AB} \qquad (\because DC = AB)$$

$$\Rightarrow \frac{PL}{DP} + 1 = \frac{BL}{AB} + 1$$

$$\Rightarrow \frac{DP + PL}{DP} = \frac{BL + AB}{AB}$$

$$\Rightarrow \frac{DL}{DP} = \frac{AL}{AB}$$

$$\Rightarrow \frac{DL}{DP} = \frac{AL}{DC}$$

(:: AB = DC)

Hence proved.

3. Given $\angle BCA = \angle ADC$

In $\triangle ACB$ and $\triangle ADC$.

$$\angle BCA = \angle ADC$$
 (Given)
 $\angle CAB = \angle DAC$ (Common angle)

(By AA similarity)

Hence proved. Also given . AC = B cm and AD = 3 cm.

We know that.

Sides of similar triangle are in same proportion.

$$\frac{AC}{AD} = \frac{AB}{AC} \implies AC^2 = AB \times AD$$

$$AB = \frac{AC^2}{AD} = \frac{(8)^2}{3} = \frac{64}{3}$$

So.
$$BD = AB - AD$$

$$=\frac{64}{3}-3=\frac{64-9}{3}=\frac{55}{3}$$

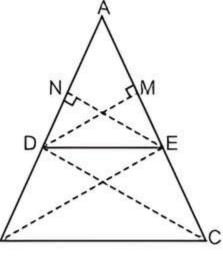
Given: In ∆ABC, DE || BC

To Prove:
$$\frac{AD}{BD} = \frac{AE}{EC}$$

Construction: Join BE and CD.

Draw DM \perp AC and EN \perp AB Proof: Here.

 $ar(\Delta ADE) = \frac{1}{2} \times AD \times EN$



(: Area of triangle =
$$\frac{1}{2}$$
 × base × height)

and
$$ar(\Delta BDE) = \frac{1}{2} \times DB \times EN$$

$$\frac{\text{ar}(\Delta ADE)}{\text{ar}(\Delta BDE)} = \frac{\frac{1}{2} \times \text{AD} \times \text{EN}}{\frac{1}{2} \times \text{DB} \times \text{EN}} = \frac{\text{AD}}{\text{DB}} \qquad \dots (1)$$

Also,
$$ar(\Delta ADE) = \frac{1}{2} \times AE \times DM$$

and $ar(\Delta DEC) = \frac{1}{2} \times EC \times DM$

$$\frac{ar(\Delta ADE)}{ar(\Delta DEC)} = \frac{\frac{1}{2} \times AE \times DM}{\frac{1}{2} \times EC \times DM} = \frac{AE}{EC}$$

Since, $\triangle BDE$ and $\triangle DEC$ are on the same base DE and between the same parallel lines BC and DE.

$$\frac{\operatorname{ar}(\Delta \mathsf{ADE})}{\operatorname{ar}(\Delta \mathsf{DEC})} = \frac{\operatorname{ar}(\Delta \mathsf{ADE})}{\operatorname{ar}(\Delta \mathsf{BDE})} = \frac{\mathsf{AE}}{\mathsf{EC}} \qquad \dots (2)$$

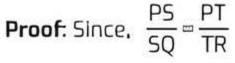
From eqs. (1) and (2).
$$\frac{AD}{DB} = \frac{AE}{FC}$$

Hence proved.

Given: In triangle PQR. S and T are points on PQ and PR respectively.

$$\frac{PS}{SQ} = \frac{PT}{TR}$$
 and $\angle PST = \angle PRQ$

To Prove: PQR is an isosceles triangle.



⇒ ST II QR

(By converse of BPT)

 $\Rightarrow \angle PST = \angle PQR$

(Corresponding angles)

$$\Rightarrow \angle PRQ = \angle PQR$$

 $[\because \angle PST = \angle PRQ \{Glven\}]$

$$\Rightarrow$$
 PQ = PR

PQ = PR (:. Sides opposite to equals angles are also equal)

 \Rightarrow \triangle PQR is an isosceles triangle. Hence proved.



Chapter Test

Multiple Choice Questions

- Q1. If in $\triangle ABC$, AB = 6 cm and $DE \parallel BC$ such that $AE = \frac{1}{4}AC$, then the length of AD is:
 - a. 2 cm
- b. 12 cm
- c. 1.5 cm
- d. 4 cm
- $\triangle MNS$, $\frac{PQ}{NS} = \frac{QR}{MS} = \frac{PR}{MN}$ Q 2. In \triangle PQR and symbolically we write as:
 - a. ΔQRP ~ ΔSMN
- b. ΔPQR~ΔSMP
- C ∆PQR ~ ∆MNS
- d. None of these

Assertion and Reason Type Questions

Directions (Q. Nos. 3-4): In the following questions, a statement of Assertion (A) is followed by a statement of Reason (R). Choose the correct option:

- a. Both Assertion (A) and Reason (R) are true and reason (R) is the correct explanation of Assertion
- b. Both Assertion (A) and Reason (R) are true but reason (R) is not the correct explanation of Assertion (A)
- c. Assertion (A) is true but Reason (R) is false
- d. Assertion (A) is false but Reason (R) is true
- Q 3. Assertion (A): ABC is a triangle in which AB = ACand D is a point on AC such that $BC^2 = AC \times CD$. Then $\triangle ABC \sim \triangle BDC$ by SAS similarity criterion.

Reason (R): If two angles of one triangle are respectively equal to the two angles of another triangle, then the two triangles are similar. This is known as SAS similarity criterion.

Q 4. Assertion (A): In a \triangle ABC, D and E are points on sides AB and AC respectively, such that BD = CE. If $\angle B = \angle C$, then DE is not parallel to BC.

Reason (R): If a line divides any two sides of a triangle in the same ratio, then the line must be parallel to the third side.

Fill in the Blanks

- Q 5. Two polygons of the same number of sides are similar, if their corresponding angles are and their corresponding sides are, in the ratio.
- Q 6. All equilateral triangles are (similar/not similar).

True/False

- Q7. Two figures having the same shapes is said to be similar figures.
- Q 8. In two triangles, if one pair of the corresponding sides are proportional and the included angles are also equal, then two triangles are not similar.

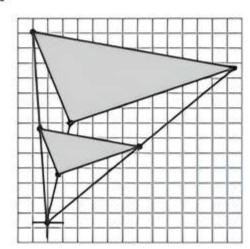
Case Study Based Question

Q 9. Scale Factor: A scale drawing of an object is of the same shape as the object but of a different dimension.

The scale of a drawing is a comparison of the length used on a drawing to the length it represents. The scale is written as a ratio.

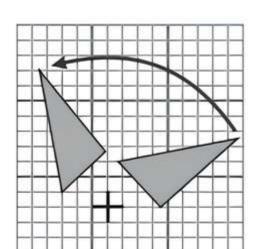
Similar Figures: The ratio of two corresponding sides in similar figures is called the scale factor.

If one shape can become another using resizing then the shapes are similar.

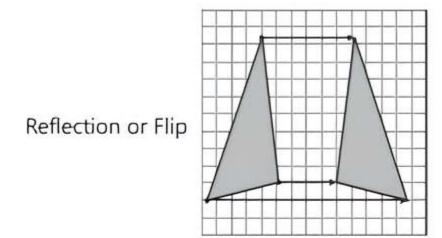


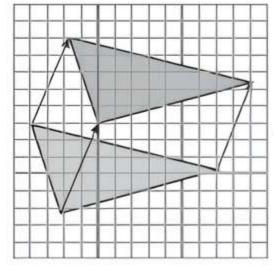






Rotation or Turn





Translation or Slide

Hence, two shapes are similar when one can become the other after a resize, flip, slide or turn. Based on the above information, solve the following questions:

(i) A model of an aeroplane is made to a scale of 1:400. Find the length (in cm) of the model, if the length of the aeroplane is 40 m.



- (ii) Find the length (in m) of the aeroplane if length of its model is 16 cm.
- (iii) A \triangle ABC has been enlarged by scale factor m=2.5to the \triangle A'B'C'. Find the length of A'B', if AB is 6 cm.

OR

Find the length of C'A', if CA = 4 cm.

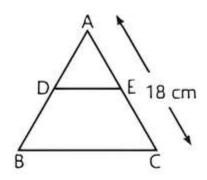
Very Short Answer Type Questions

- Q10. If the corresponding altitudes of two similar triangles are in the ratio 3:5, then find the ratio of their corresponding sides.
- Q 11. If in triangles ABC and DEF, $\frac{AB}{DF} = \frac{BC}{FD}$ and \angle B = \angle D, then these triangles will be similar by which criteria?

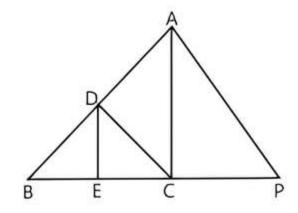
Short Answer Type-I Questions

Q 12. In the given figure, DE || BC. If $\frac{AD}{DB} = \frac{2}{3}$ and

AC = 18 cm, find AE.

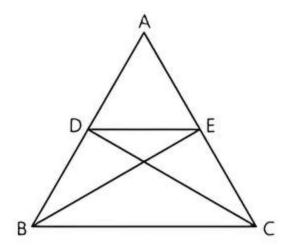


Q 13. In the given figure, DE || AC and DC || AP. Prove that $\frac{BC}{CP} = \frac{BE}{EC}$.



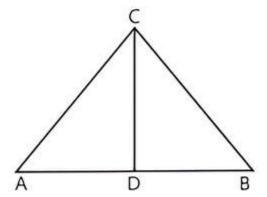
Short Answer Type-II Questions

Q 14. In the given figure, if $\triangle ABE \cong \triangle ACD$, prove that $\triangle ADE \sim \triangle ABC$.



Q 15. In the given figure, \angle ACB = 90° and CD \perp AB. Prove

that
$$\frac{CB^2}{CA^2} = \frac{BD}{AD}$$



Long Answer Type Question

Q 16. Through the vertex D of a parallelogram ABCD, a line is drawn to intersect the sides BA and BC produced at E and F respectively. Prove that

$$\frac{DA}{AE} = \frac{FB}{BE} = \frac{FC}{CD}$$
.